

verifying SHA using VST

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last paper in the reading list of

Type Theory & Coq

2015–2016

Radboud University Nijmegen

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SHA and VST

- ▶ SHA =
Secure Hash Algorithm
- ▶ VST =
Verified Software Toolchain

papers by Andrew Appel:

- ▶ **Verification of a Cryptographic Primitive: SHA-256**
TOPLAS = ACM Transactions on Programming Languages
and Systems
April 2015
- ▶ **Second Edition: Verification of a Cryptographic Primitive:
SHA-256**
updated from VST 1.0 to VST 1.6

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- ▶ **Second Edition: Verification of a Cryptographic Primitive:
SHA-256**
updated from VST 1.0 to VST 1.6
- ▶ **Modular Verification for Computer Security**
CSF 2016 = Computer Security Foundations Symposium
June 2016

recap reading list

overview

- ▶ **imp**
 - ▶ big-step operational semantics
 - ▶ small-step operational semantics
 - ▶ Hoare logic
 - ▶ verification condition generator
- ▶ **CompCert**
 - ▶ idem for C
- ▶ **VST**
 - ▶ separation logic
 - ▶ symbolic execution

imp

syntax:

$a ::= n \mid x \mid (a_1 + a_2) \mid (a_1 - a_2) \mid (a_1 \cdot a_2)$

$b ::= a_1 = a_2 \mid a_1 < a_2 \mid \top \mid \neg b \mid (b_1 \wedge b_2)$

$c ::= \text{skip} \mid x := a \mid (c_1; c_2) \mid \text{if } b \text{ then } c_1 \text{ else } c_2 \text{ fi} \mid \text{while } b \text{ do } c \text{ od}$

example:

```
(i := 1;  
 f := 1);  
while i < n do  
  i := i + 1;  
  f := f · i  
od
```

big-step operational semantics

= natural semantics

Gilles Kahn

relation:

$$(c, s) \Downarrow s'$$

some representative rules:

$$\frac{(a, s) \Downarrow n}{(x := a, s) \Downarrow s[x \mapsto n]}$$

$$\frac{(c_1, s) \Downarrow s' \quad (c_2, s') \Downarrow s''}{(c_1; c_2, s) \Downarrow s''}$$

$$\frac{(b, s) \Downarrow \top \quad (c, s) \Downarrow s' \quad (\text{while } b \text{ do } c \text{ od}, s') \Downarrow s''}{(\text{while } b \text{ do } c \text{ od}, s) \Downarrow s''}$$

$$\frac{(b, s) \Downarrow \perp}{(\text{while } b \text{ do } c \text{ od}, s) \Downarrow s}$$

small-step operational semantics

= structural operational semantics = SOS

Gordon Plotkin

relations:

$$(c, s) \rightarrow (c', s') \quad (c, s) \rightarrow^* (c', s')$$

some representative rules:

$$\frac{(a, s) \rightarrow (a', s)}{(x := a, s) \rightarrow (x := a', s)}$$

$$\frac{}{(x := n, s) \rightarrow (\text{skip}, s[x \mapsto n])}$$

$$\frac{(c_1, s) \rightarrow (c'_1, s')}{(c_1; c_2, s) \rightarrow (c'_1; c_2, s')}$$

$$\frac{}{(\text{skip}; c_2, s) \rightarrow (c_2, s)}$$

$$\frac{}{(\text{while } b \text{ do } c \text{ od}, s) \rightarrow (\text{if } b \text{ then } c; \text{ while } b \text{ do } c \text{ od else skip fi}, s)}$$

Hoare logic

= axiomatic semantics

Tony Hoare

Hoare triple:

$$\{P\} c \{Q\}$$

some representative rules:

$$\begin{array}{c} \overline{\{Q[x := a]\} x := a \{Q\}} \\[1em] \frac{\{P\} c_1 \{Q\} \quad \{Q\} c_2 \{R\}}{\{P\} c_1; c_2 \{R\}} \\[1em] \frac{\{P \wedge b\} c \{P\}}{\{P\} \text{ while } b \text{ do } c \text{ od } \{P \wedge \neg b\}} \\[1em] \frac{P \Rightarrow P' \quad \{P'\} c \{Q'\} \quad Q' \Rightarrow Q}{\{P\} c \{Q\}} \end{array}$$

verification conditions from weakest preconditions

predicate transformer semantics

Edsger Dijkstra

imp with annotations:

$$\bar{c} ::= \{P\} \mid \text{skip} \mid x := a \mid (\bar{c}_1; \bar{c}_2) \mid \text{if } b \text{ then } \bar{c}_1 \text{ else } \bar{c}_2 \text{ fi} \mid \\ \text{while } b \text{ do } \{P\} \bar{c} \text{ od}$$

verification condition and weakest precondition:

$$vc(\{P\} \bar{c} \{Q\}) = (P \Rightarrow wp(\bar{c}, Q))$$

some representative cases:

$$wp(\{P\}, Q) = P \wedge Q$$

$$wp(x := a, Q) = Q[x := a]$$

$$wp(\bar{c}_1; \bar{c}_2, Q) = wp(\bar{c}_1, wp(\bar{c}_2, Q))$$

$$wp(\text{while } b \text{ do } \{P\} \bar{c} \text{ od}, Q) = P \wedge (P \wedge b \Rightarrow wp(\bar{c}, P)) \wedge (P \wedge \neg b \Rightarrow Q)$$

CompCert

Xavier Leroy, INRIA, France

CompCert = idem for C

- ▶ C to Clight translator in OCaml
- ▶ optimizing Clight **compiler** as a Coq function
- ▶ Coq code extracted to OCaml
- ▶ operational semantics of Clight in Coq
- ▶ operational semantics of assembly in Coq
- ▶ compiler proved correct in Coq



separation logic

Hoare logic for pointers in memory

John Reynolds and Peter O'Hearn

$$\text{state} = \text{store} \times \text{heap}$$

$$\text{store} = \text{ident} \rightarrow \mathbb{Z}$$

$$\text{heap} = \mathbb{Z} \multimap \mathbb{Z}$$

separation logic assertions:

emp

$$a_1 \mapsto a_2$$

$$P * Q$$

frame rule:

$$\frac{\{P\} c \{Q\}}{\{P * R\} c \{Q * R\}}$$

VST

Andrew Appel, Princeton, US



VST

= Verified Software Toolchain

= CompCert +

- ▶ separation logic
- ▶ semantics for separate compilation
- ▶ **symbolic execution**
 - ▶ Coq goal is a Hoare triple
 - ▶ tactics execute statements

SHA hashing

SSL, TLS and OpenSSL

OpenSSL

= open source implementation of SSL and TLS protocols

used by majority of the web servers

SSL = Secure Socket Layer

TLS = Transport Layer Security

secure communication on the internet

private connection: symmetric cryptography

identity checking: public-key cryptography

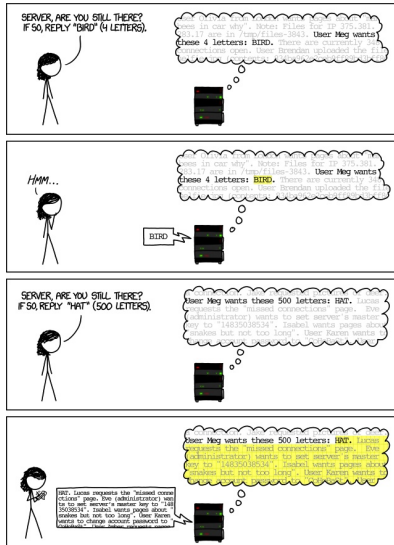
reliable connection

HTTPS = HTTP + TLS

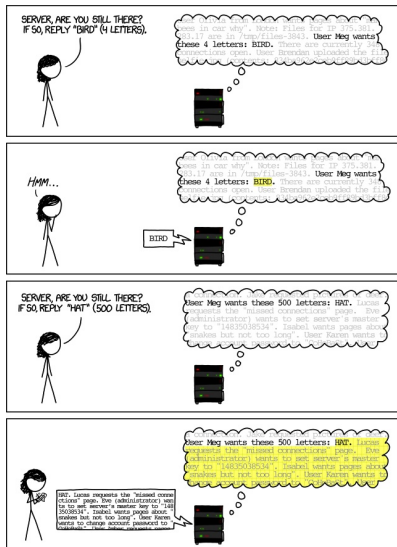
heartbleed



April 2014



heartbleed



April 2014

fix is two lines in
ssl/d1_lib.c:

```
if (HEARTBEAT_SIZE_STD  
    (payload) > length)  
    return 0;  
/* silently discard per  
   RFC 6520 sec. 4 */
```

cryptographic hashing

cryptographic hash function:

$$h : \{0, 1\}^* \rightarrow \{0, 1\}^{256}$$

four properties:

- ▶ $h(x)$ can be computed quickly
- ▶ given $h(x)$ finding a corresponding x is infeasible
- ▶ small change in x gives a large change in $h(x)$
- ▶ infeasible to find a **collision**: x_1 and x_2 with $h(x_1) = h(x_2)$

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examples:

```
h("Lynx c.q. vos prikt bh: dag zwemjuf") =  
17c2f3484ab21559fa8d7bf3da97e3443b48a3466f3b8fa8210dbcefe99807a1  
h("Lynx c.q. vos prikt bh: dag zwemjuf!") =  
3530df7cc04da1f245eb92e5780610c5e0aa066a94ba17a66e2e310a64f1bd4d
```

SHA-256 and HMAC

SHA = Secure Hash Algorithm

SHA-0: 1993, SHA-1: 1995, **SHA-2**: 2001, SHA-3: 2015

SHA-0: collision known

SHA-1: collision unknown, but within range of supercomputers

SHA-2 = FIPS PUB 180-2 standard of NIST =

SHA-224, **SHA-256**, SHA-384, SHA-512, SHA-512/224, SHA-512/256

SHA-256: used by bitcoin

SHA-256 and HMAC

SHA = Secure Hash Algorithm

SHA-0: 1993, SHA-1: 1995, SHA-2: 2001, SHA-3: 2015

SHA-0: collision known

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SHA-2 = FIPS PUB 180-2 standard of NIST =

SHA-224, SHA-256, SHA-384, SHA-512, SHA-512/224, SHA-512/256

SHA-256: used by bitcoin

HMAC = Hash-based Message Authentication Code

- ▶ authenticity: message came from sender
- ▶ integrity: message has not been tampered with

VST example: verifying factorial

workflow

VST example: verifying factorial

workflow

- ▶ `fac.c`
C program being verified
 - ▶ `fac`
C function calculating factorial

VST example: verifying factorial

workflow

- ▶ `fac.c`
C program being verified
 - ▶ `fac`
C function calculating factorial
- ▶ `fac.v`
Clight version as a generated Coq file

VST example: verifying factorial

workflow

- ▶ `fac.c`
C program being verified
 - ▶ `fac`
C function calculating factorial
- ▶ `fac.v`
Clight version as a generated Coq file
- ▶ `verif_fac.v`
Coq file with the verification

VST example: verifying factorial

workflow

- ▶ `fac.c`

C program being verified

- ▶ `fac`

C function calculating factorial

- ▶ `fac.v`

Clight version as a generated Coq file

- ▶ `verif_fac.v`

Coq file with the verification

- ▶ `FAC`

Coq functional program for each function in `fac.c`

- ▶ `fac_spec`

specification relating each function in `fac.c` to its Coq version

- ▶ `body_fac`

verification of correctness of each function in `fac.c`

fac.c

10 lines of C
calculates the factorial function

```
int
fac(int n)
{
    int i, f;

    f = i = 1;
    while (i < n)
        f *= ++i;
    return f;
}
```

320 lines of Coq, **generated** from fac.c by CompCert's `clightgen`

```
...
Definition _n : ident := 45%positive. ...
Definition _fac : ident := 48%positive. ...

Definition f_fac := {|
  fn_return := tint;
  fn_callconv := cc_default;
  fn_params := ((_n, tint) :: nil);
  fn_vars := nil;
  fn_temps := ((_i, tint) :: (_f, tint) :: (51%positive, tint) ::
               (50%positive, tint) :: nil);
  fn_body := (Ssequence (Ssequence ... ...) ...)
|}.

...
Definition prog : Clight.program := {|
  prog_defs := (... :: (_fac, Gfun(Internal, f_fac)) :: nil);
  ...
|}.
```

verif_fac.v

59 lines of Coq

checking time: 75 seconds

verif_fac.v

59 lines of Coq

checking time: 75 seconds

full code in these slides

starts with imports:

```
Require Import floyd.proofauto.  
Require Import Coqlib.  
Require Import Recdef.
```

FAC

implementation of factorial in Coq using Function
(recursion on Acc well-foundedness predicate):

```
Function FAC (i : Z) {measure Z.to_nat i} : Z :=  
  if zle i 1 then 1 else FAC (i - 1) * i.
```

FAC

implementation of factorial in Coq using Function
(recursion on Acc well-foundedness predicate):

```
Function FAC (i : Z) {measure Z.to_nat i} : Z :=  
  if zle i 1 then 1 else FAC (i - 1) * i.  
Proof. intros. apply Z2Nat.inj_lt; omega. Defined.
```

FAC

implementation of factorial in Coq using Function
(recursion on Acc well-foundedness predicate):

```
Function FAC (i : Z) {measure Z.to_nat i} : Z :=  
  if zle i 1 then 1 else FAC (i - 1) * i.  
Proof. intros. apply Z2Nat.inj_lt; omega. Defined.
```

and a trivial lemma that we will need later
(functions defined with Function do not reduce well):

```
Lemma FAC_step (i : Z) :  
  i > 0 -> FAC (i + 1) = FAC i * (i + 1).  
Proof.  
  intros. rewrite FAC_equation. destruct (zle (i + 1) 1).  
  omega. assert (i + 1 - 1 = i). omega. rewrite H0. auto.  
Qed.
```

fac_spec

importing definitions from the generated `fac.v`:

```
Require Import fac.fac.
```

and the specification of our function:

```
Definition fac_spec :=  
  DECLARE _fac  
    WITH n : Z  
    PRE [ _n OF tint ]  
      PROP (0 <= n <= Int.max_signed)  
      LOCAL (temp _n (Vint (Int.repr n)))  
      SEP ()  
    POST [ tint ]  
      PROP ()  
      LOCAL (temp ret_temp (Vint (Int.repr (FAC n))))  
      SEP ().
```

PROP and LOCAL and SEP

assertions P consist of three parts:

- ▶ PROP

does not refer to store or heap

$$(!b) s h := \text{emp } s h \wedge b$$

- ▶ LOCAL

refers only to store

$$(!b) s h := \text{emp } s h \wedge \text{eval}(b, s)$$

- ▶ SEP

refers to both store and heap

$$(b) s h$$

temp and data_at

two basic assertions

- ▶ LOCAL assertion:

$$s(x) = n$$

temp $x\ n$

- ▶ SEP assertion:

$$a_1 \mapsto a_2$$

data_at $\pi\ \tau\ a_2\ a_1$

τ = C type

π = permission

body_fac

'boilerplate' to define some variables related to prog:

Instance CompSpecs : compspecs. make_compspecs prog. Defined.

Definition Vprog : varsspecs. mk_varspecs prog. Defined.

Definition Gprog := augment_funspecs prog [fac_spec].

body_fac

'boilerplate' to define some variables related to prog:

```
Instance CompSpecs : compspecs. make_compspecs prog. Defined.  
Definition Vprog : varspecs. mk_varspecs prog. Defined.  
Definition Gprog := augment_funspecs prog [fac_spec].
```

correctness of the body of fac, using symbolic execution:

```
Lemma body_fac: semax_body Vprog Gprog f_fac fac_spec.  
Proof.  
  start_function. forward. forward. forward.  
  forward_while (fac_inv n). Exists 1. entailer!. entailer!.  
    forward. forward. forward. Exists (i + 1). entailer!.  
    split. omega. rewrite FAC_step. auto. omega.  
  forward.  
  destruct H0. assert (i = n). omega. subst. entailer!.  
  destruct H0. subst. entailer!.  
Qed.
```

`all_funcs_correct`

more 'boilerplate':

```
Existing Instance NullExtension.Espec.
```

including the correctness of the program
(combining the correctness of all functions):

```
Lemma all_funcs_correct :
```

```
  semax_func Vprog Gprog (prog_funct prog) Gprog.
```

```
Proof.
```

```
unfold Gprog, prog, prog_funct. semax_func_cons body_fac.
```

```
Qed.
```

fac_inv

the loop invariant that we had skipped
(this finishes the code from `verif_fac.v`):

```
Definition fac_inv (n : Z) : environ -> mpred :=  
  EX i : Z,  
    PROP (1 <= i <= n \/ (n = 0 /\ i = 1))  
    LOCAL (temp _n (Vint (Int.repr n));  
           temp _i (Vint (Int.repr i));  
           temp _f (Vint (Int.repr (FAC i))))  
    SEP  ().
```

annotated program

```
{ $0 \leq n \leq 2^{31} - 1$ }  
 $i := 1$ ;  
 $f := 1$ ;  
while  $i < n$  do  $\{(1 \leq i \leq n \vee (n = 0 \wedge i = 1)) \wedge f = i!\}$   
     $i := i + 1$ ;  
     $f := f \cdot i$   
od  
 $\{f = n!\}$ 
```

annotated program

```
 $\{0 \leq n \leq 2^{31} - 1\}$   
 $i := 1;$   
 $f := 1;$   
while  $i < n$  do  $\{(1 \leq i \leq n \vee (n = 0 \wedge i = 1)) \wedge f = i!\}$   
     $i := i + 1;$   
     $f := f \cdot i$   
od  
 $\{f = n!\}$ 
```

verification conditions:

```
 $0 \leq n \leq 2^{31} - 1$   
 $\Rightarrow (1 \leq 1 \leq n \vee (n = 0 \wedge 1 = 1)) \wedge 1 = 1!$   
 $(1 \leq i \leq n \vee (n = 0 \wedge i = 1)) \wedge f = i! \wedge i < n$   
 $\Rightarrow (1 \leq i + 1 \leq n \vee (n = 0 \wedge i + 1 = 1)) \wedge f \cdot (i + 1) = (i + 1)!$   
 $(1 \leq i \leq n \vee (n = 0 \wedge i = 1)) \wedge f = i! \wedge \neg(i < n)$   
 $\Rightarrow f = n!$ 
```

DEMO

verifying SHA-256

sha.c in VST

counterpart of OpenSSL crypto/sha/sha256.c

247 lines of code, 1 typedef, 1 const array, 6 functions

```
typedef struct SHA256state_st {...} SHA256_CTX;  
static const unsigned int K256[64] = ...;  
  
void sha256_block_data_order(SHA256_CTX *ctx, const void *in)  
void SHA256_addlength(SHA256_CTX *c, size_t len)  
void SHA256_Init(SHA256_CTX *c)  
void SHA256_Update(SHA256_CTX *c, const void *data_, size_t len)  
void SHA256_Final(unsigned char *md, SHA256_CTX *c)  
void SHA256(const unsigned char *d, size_t n, unsigned char *md)
```

fragment of sha256_block_data_order

after macro preprocessing:

```
...
for (i = 0; i < 16; i++) {
    l1 = (((unsigned long) (*((data)++))) << 24), l1 |=
        (((unsigned long) (*((data)++))) << 16), l1 |=
        (((unsigned long) (*((data)++))) << 8), l1 |=
        (((unsigned long) (*((data)++)))), l1);
    X[i] = l1;
    Ki = K256[i];
    T1 = l1 + h + (((((e)) << (26)) | (((e)) & 0xffffffff) >> (32 - (26)))) ^
        (((e)) << (21)) | (((e)) & 0xffffffff) >> (32 - (21))) ^
        (((e)) << (7)) | (((e)) & 0xffffffff) >> (32 - (7)))) +
        ((e) & (f)) ^ ((~(e)) & (g))) + Ki;
    T2 = (((((a)) << (30)) | (((a)) & 0xffffffff) >> (32 - (30)))) ^
        (((a)) << (19)) | (((a)) & 0xffffffff) >> (32 - (19))) ^
        (((a)) << (10)) | (((a)) & 0xffffffff) >> (32 - (10)))) +
        (((a) & (b)) ^ ((a) & (c)) ^ ((b) & (c)));
    h = g; g = f; f = e; e = d + T1;
    d = c; c = b; b = a; a = T1 + T2;
}
...
```

an array on the stack

another fragment of sha256_block_data_order:

```
#define SHA_LONG unsigned int

void sha256_block_data_order (SHA256_CTX *ctx, const void *in)
{
    unsigned MD32_REG_T a,b,c,d,e,f,g,h,s0,s1,T1,T2,t;
    SHA_LONG X[16],l,Ki;
    int i;
    const unsigned char *data=in;
    ...
}
```

some other frameworks cannot handle local array variables!

fac versus sha

- ▶ counterpart of `fac.c` is `sha.c`
- ▶ counterpart of `fac.v` is `sha.v`
- ▶ counterparts of `verif_fac.v`:
 - ▶ counterpart of `FAC` is the file `SHA256.v` with:
 - ▶ `SHA_256`
 - ▶ counterpart of `fac_spec` is the file `spec_sha.v` with:
 - ▶ `sha256_block_data_order_spec`
 - ▶ `SHA256_addlength_spec`
 - ▶ `SHA256_Init_spec`
 - ▶ `SHA256_Update_spec`
 - ▶ `SHA256_Final_spec`
 - ▶ `SHA256_spec`
 - ▶ counterparts of `body_fac` are the files:
 - ▶ `verif_sha_bdo.v` with `body_sha256_block_data_order`
 - ▶ `verif_addlength.v` with `body_SHA256_addlength`
 - ▶ `verif_sha_init.v` with `body_SHA256_Init`
 - ▶ `verif_sha_update.v` with `body_SHA256_Update`
 - ▶ `verif_sha_final.v` with `body_SHA256_Final`
 - ▶ `verif_SHA256.v` with `body_SHA256`
- ▶ *plus several other files with lots of lemmas*

two executable versions

Fibonacci function with naive recursion takes exponential time

two executable versions

Fibonacci function with naive recursion takes exponential time

- ▶ `SHA256.v` defines `SHA256`
naive implementation
exponential time
- ▶ `functional_prog.v` defines `SHA256'`
better implementation
reasonable time
about a million times slower than C implementation
- ▶ ... and proves `SHA256' = SHA256`

testing on examples: seem okay

sizes and times

lines	seconds	component
842	17	lemmas about the functional spec
756	27	lemmas about the API spec
1613	47	verification of sha256_block_data_order
251	61	verification of SHA256_addlength
34	102	verification of SHA256_Init
1745	658	verification of SHA256_Update
1276	781	verification of SHA256_Final
37	38	verification of SHA256
6555	2358	total

trusting the spec

why trust that the spec is correct?

- ▶ C program: `sha.c`
268 lines
- ▶ Coq specification: `SHA256.v` + `spec_sha.v`
 $154 + 210 = 364$ lines

trust

trusting the spec

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- ▶ C program: `sha.c`
268 lines
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 $154 + 210 = 364$ lines

possible to **prove** crypto properties of the Coq definitions

is it really OpenSSL?

changes in the code:

- ▶ macros expanded to the SHA-256 case
- ▶ compiled to Clight in a specific way
- ▶ adapted: no side effects inside subexpressions
- ▶ adapted: no memory references inside subexpressions
- ▶ some additional return statements

current version of OpenSSL not close to this any more

trusted computing base

VST framework

- ▶ CompCert semantics of C
'is it really C?'
(**not** part of TCB when compiling using CompCert)
- ▶ CompCert semantics of assembly
- ▶ Calculus of Inductive Constructions
- ▶ source code of Coq **kernel**
- ▶ source code of OCaml compiler and runtime
- ▶ microprocessor

SHA correctness

- ▶ **SHA specification**
- ▶ C compiler
(**not** part of TCB when compiling using CompCert)
- ▶ assembler
- ▶ microprocessor

axioms

```
Print Assumptions all_funcs_correct.
```

axioms

Print Assumptions all_funcs_correct.

- ▶ `Classical_Prop.classic` :
forall P : Prop, P $\backslash$ / ~ P
- ▶ `prop_ext` :
forall A B : Prop, (A $\leftrightarrow$ B) $\rightarrow$ A = B
- ▶ `functional_extensionality_dep` :
forall (A : Type) (B : A $\rightarrow$ Type)
 (f g : forall x : A, B x),
 (forall x : A, f x = g x) $\rightarrow$ f = g

Print Assumptions `all_funcs_correct`.

- ▶ `Classical_Prop.classic` :
forall $P : \text{Prop}$, $P \wedge \sim P$
- ▶ `prop_ext` :
forall $A B : \text{Prop}$, $(A \leftrightarrow B) \rightarrow A = B$
- ▶ `functional_extensionality_dep` :
forall $(A : \text{Type}) (B : A \rightarrow \text{Type})$
 $(f\ g : \text{forall } x : A, B\ x),$
 $(\text{forall } x : A, f\ x = g\ x) \rightarrow f = g$
- ▶ **26 axioms** about real numbers
 through CompCert (floating point) through Floc

Print Assumptions `all_funcs_correct`.

- ▶ `Classical_Prop.classic` :
forall P : Prop, P $\backslash$ / ~ P
- ▶ `prop_ext` :
forall A B : Prop, (A $\leftrightarrow$ B) $\rightarrow$ A = B
- ▶ `functional_extensionality_dep` :
forall (A : Type) (B : A $\rightarrow$ Type)
 (f g : forall x : A, B x),
 (forall x : A, f x = g x) $\rightarrow$ f = g
- ▶ **26 axioms** about real numbers
through CompCert (floating point) through Floc
- ▶ **19 axioms** about semax
proved in `veric/SeparationLogicSoundness.v`
(‘I didn’t want to complicate things with a Functor application
somewhere’)

$$17! = -288522240?$$

%

$17! = -288522240?$

% factest

$17! = -288522240?$

% factest

17

$17! = -288522240?$

% factest

17

-288522240

%

17! = -288522240?

% factest

17

-288522240

%

- ▶ overflow in C11 standard: *undefined behavior* = crash
(computer can do whatever it likes)
- ▶ overflow in CompCert: wraps mod 2^{32}
(in that case: the computer likes to wrap 😊)
- ▶ **but didn't we prove that the program calculates $n!$?**
(where is the 'modulo' in the specification?)

17! = -288522240?

```
% factest  
17  
-288522240  
%
```

- ▶ overflow in C11 standard: *undefined behavior* = crash (computer can do whatever it likes)
- ▶ overflow in CompCert: wraps mod 2^{32} (in that case: the computer likes to wrap 😊)
- ▶ **but didn't we prove that the program calculates $n!$?** (where is the 'modulo' in the specification?)

$$s(x) = n$$

```
temp x (Vint (Int.repr n))
```

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- ▶ overflow in C11 standard: *undefined behavior* = crash (computer can do whatever it likes)
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- ▶ **but didn't we prove that the program calculates $n!$?** (where is the 'modulo' in the specification?)

$s(x) = n$
`temp x (Vint (Int.repr n))`

not: 'the value of x is n '

but: 'the value of x is the residue of n mod 2^{32} '

related work

specification, implementation, foundational, automatic, general

- ▶ **specification**

is there a specification of the program's function?
amenable to analysis in a proof assistant?

- ▶ **implementation**

is the proof about an efficient implementation?

- ▶ **foundational**

is there an end-to-end machine-checked proof from the
foundations of logic?

- ▶ **automatic** (VST: ☹)

check or synthesize the program without much interactive
human input or annotations?

- ▶ **general**

can the verifier handle all parts of the program?

larger C verification projects

two recent large C verification projects

- ▶ **seL4 in Isabelle**

Gerwin Klein et al. 2009

NICTA, Australia

- ▶ **CertiKOS in Coq**

Liang Gu et al. 2011

Yale, US

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but:

- ▶ no separation logic
- ▶ no function pointers/higher order specifications
- ▶ seL4 and CertKOS: newly written code
- ▶ **no arrays on the stack**

who has choices need not choose

different approaches to program verification:

- ▶ static analysis
- ▶ model checking
- ▶ **interactive theorem provers**
type theory!

table of contents

contents

recap reading list

SHA hashing

VST example: verifying factorial

verifying SHA-256

trust

related work

table of contents