

# Beyond $2^{c/2}$ Security in Sponge-Based Authenticated Encryption Modes

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<sup>1</sup> Universität Passau

<sup>2</sup> KU Leuven



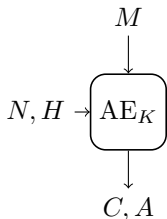
DIAC — August 23, 2014

# Authenticated Encryption

- Encryption and authentication in one
- Applications: SSH, IPsec, TLS, IEEE 802.11
- CAESAR competition

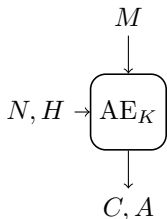
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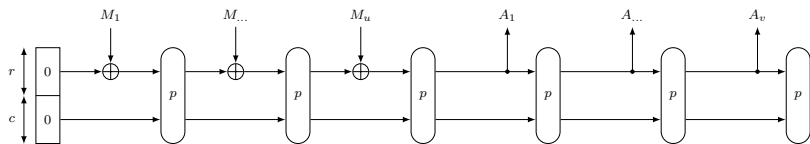
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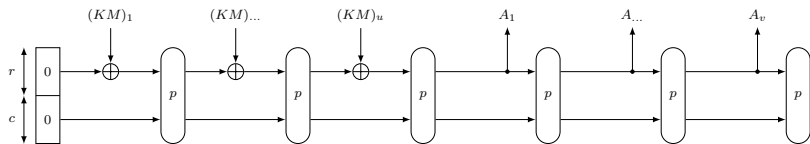
- Security goals: privacy + integrity
  - Nonce-dependent or security against nonce-reuse

# Sponge Functions



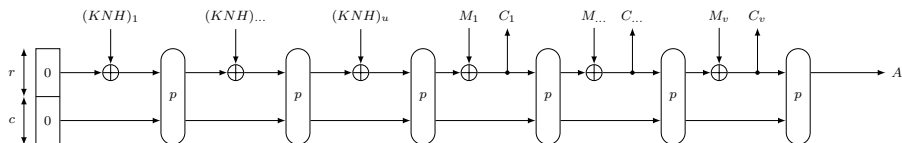
- Bertoni, Daemen, Peeters, and Van Assche (2007)
- Based on permutation  $p$
- $b = r + c$

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- AE: SpongeWrap (duplexing mode)

# Sponge Functions

**Sponge (hash)**

$2^{c/2}$  security

$c$  = capacity

$\kappa$  = key size

$\tau$  = tag size



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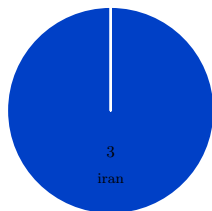
# Sponge Functions

<b>Sponge (hash)</b>	$2^{c/2}$ security
<b>Keyed sponge (MAC)</b>	$\min\{2^{c-a}, 2^\kappa\}$ security ( $2^a$ offline compl.) $\approx \min\{2^{c/2}, 2^\kappa\}$ security
<b>SpongeWrap (AE)</b>	$\min\{2^{c/2}, 2^\kappa\}$ security (privacy) $\min\{2^{c/2}, 2^\kappa, 2^\tau\}$ security (integrity)

$c$  = capacity       $\kappa$  = key size       $\tau$  = tag size

# Sponge-Based CAESAR Modes

Artemia



Ascon



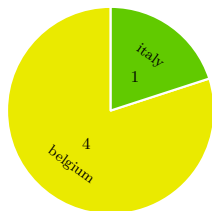
CBEAM&STRIBOB



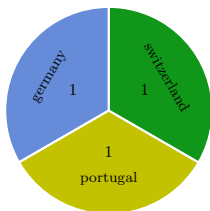
ICEPOLE



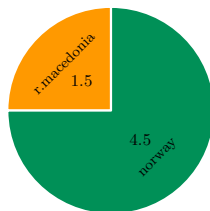
Ketje&Keyak



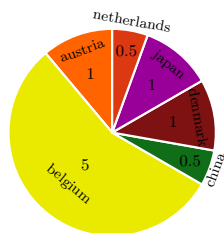
NORX



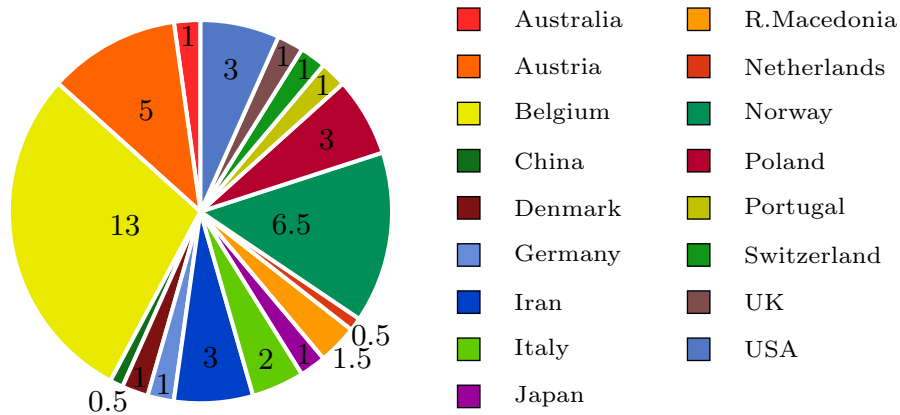
$\pi$ -Cipher



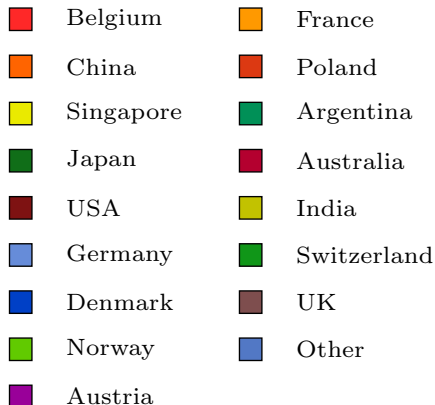
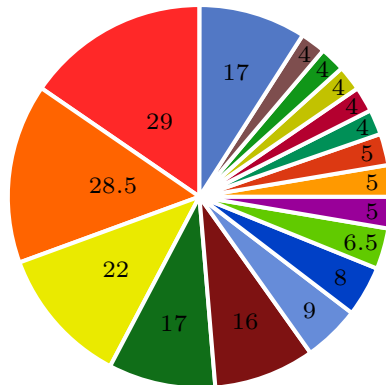
PRIMATEs



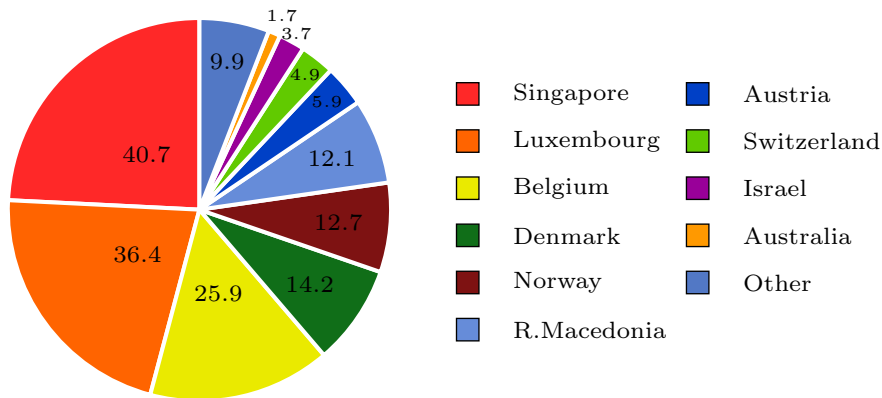
## Sponge-Based CAESAR Modes



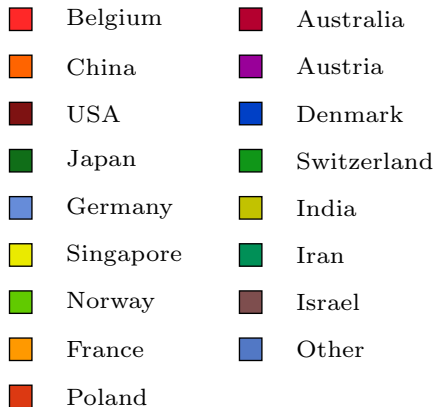
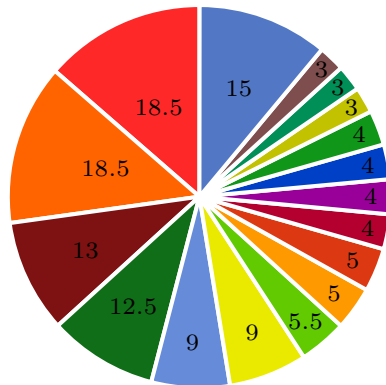
## Intermezzo – All CAESAR Contributors



## Intermezzo – All CAESAR Contributors (10.000.000/capita)



## Intermezzo – All CAESAR Contributors (no duplicate)





# Sponge-Based CAESAR Modes

<b>nonce-dependent</b>	<b>security against nonce-reuse</b>
Artemia	APE <sup>2,3</sup>
Ascon	
CBEAM/STRIBOB <sup>1</sup>	
ICEPOLE	
Ketje	
Keyak	
NORX	
$\pi$ -Cipher	
GIBBON/HANUMAN <sup>2</sup>	

<sup>1</sup> CBEAM and STRIBOB use BLNK sponge mode

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$2^c/2$  security  
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parameters based on $2^{c/2}$ and $(2^a, 2^{c-a})$ results	Artemia	APE <sup>2,3</sup>
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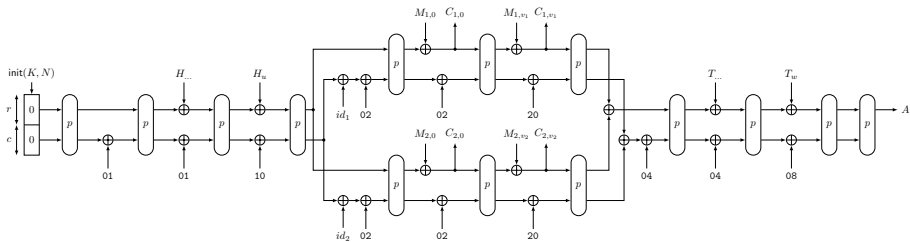
<sup>3</sup> also used in submission Prøst

**Nonce changes everything!**

# Sponge-Based CAESAR Modes

	$b$	$c$	$r$	$\kappa$	security
Ascon	320	192	128	96	<b>96</b>
	320	256	64	128	<b>128</b>
CBEAM	256	190	66	128	<b>128</b>
ICEPOLE	1280	254	1026	128	<b>128</b>
	1280	318	962	256	<b>256</b>
Keyak	800	252	548	128	<b>128</b>
	1600	252	1348	128	<b>128</b>
NORX	512	192	320	128	<b>128</b>
	1024	384	640	256	<b>256</b>
GIBBON/ HANUMAN	200	159	41	80	<b>80</b>
	280	239	41	120	<b>120</b>
STRIBOB	512	254	258	192	<b>192</b>

# NORX



- Submission by Aumasson, Jovanovic, and Neves
- Initialization with  $K$  and unique  $N$
- Header – message – trailer
- Parallelism  $D \in \{0, \dots, 255\}$  (here,  $D = 2$ )

# NORX: Mode Security

## Privacy

$\min\{2^{b/2}, 2^c, 2^\kappa\}$  security

## Integrity

$\min\{2^{b/2}, 2^c, 2^\kappa, 2^\tau\}$  security

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## Main Implication

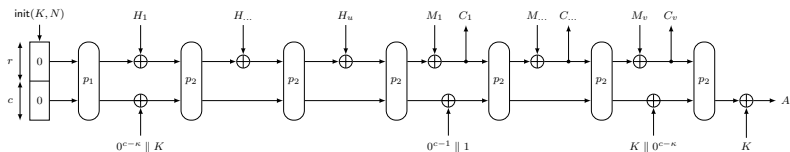
putting  $c = \kappa$  does not decrease mode security level



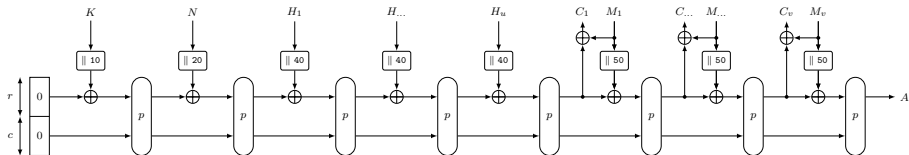
# Generalization

- Generalizes to SpongeWrap and DuplexWrap
- Generalizes to CAESAR submission **modes**
  - Ascon
  - BLNK (used in CBEAM and STRIBOB)
  - ICEPOLE
  - Keyak
  - GIBBON and HANUMAN (two PRIMATEs)

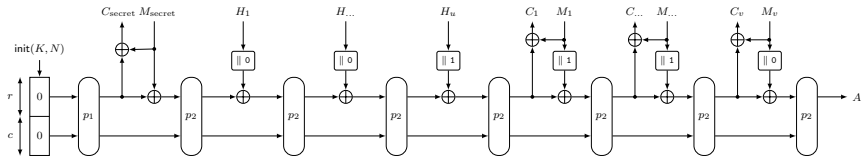
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Ascon

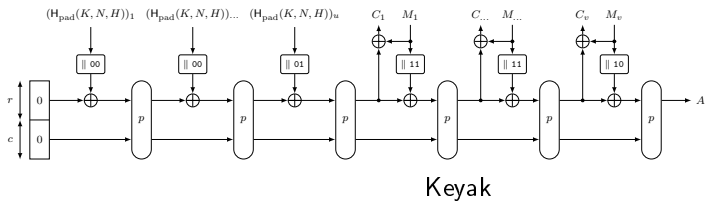


BLNK (used in CBEAM and STRIBOB)

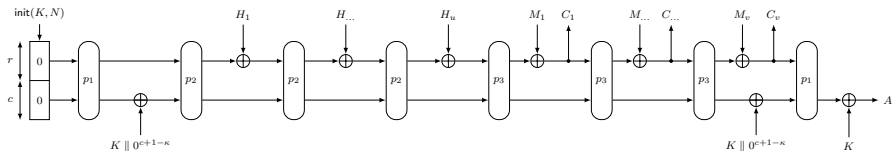


ICEPOLE

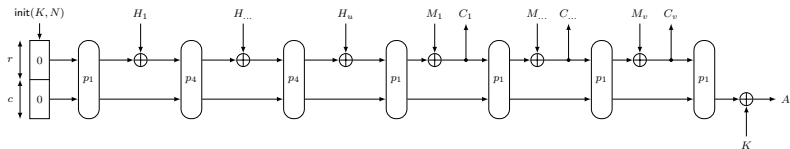
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Keyak



GIBBON (PRIMATEs)



HANUMAN (PRIMATEs)

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STRIBOB	512	192	320	1.24	192	192

# Conclusions

From  $\min\{2^{c/2}, 2^\kappa\}$  to  $\min\{2^{b/2}, 2^c, 2^\kappa\}$

- Applies to
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**Thank you for your attention!**

<http://eprint.iacr.org/2014/373>

# SUPPORTING SLIDES

## NORX: Privacy

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  - Random permutation  $p$ , key  $K$ , and AE  $\$$
  - Define  $m = \text{total complexity} = q + \sigma_\mathcal{E}$

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### Security Model

- Adversary with access to  $(p, \mathcal{E}_K^p, \mathcal{D}_K^p)$  aims to forge
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- Collisions **not** involving  $\mathcal{D}$ -state  $\rightarrow \sigma_{\mathcal{E}}^2/2^b + \rho q/2^c$
- Collisions involving  $\mathcal{D}$ -state  $\rightarrow m\sigma_{\mathcal{D}}/2^c$  (nonce re-use)

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- Collisions involving  $\mathcal{D}$ -state  $\rightarrow m\sigma_\mathcal{D}/2^c$  (nonce re-use)  
 $\sigma_\mathcal{D}$  relatively small



# NORX: Integrity

$$\min\{2^{b/2}, 2^c, 2^\kappa, 2^\tau\} \text{ security}$$

## Security Model

- Adversary with access to  $(p, \mathcal{E}_K^p, \mathcal{D}_K^p)$  aims to forge
  - Random permutation  $p$  and key  $K$
  - Define  $m = \text{total complexity} = q + \sigma_{\mathcal{E}} + \sigma_{\mathcal{D}}$
- Technical issue: adversary can re-use nonce!

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- Collisions involving  $\mathcal{D}$ -state  $\rightarrow m\sigma_{\mathcal{D}}/2^c$  (nonce re-use)  
 $\sigma_{\mathcal{D}}$  relatively small
- As long as no collisions, forgery  $\rightarrow \sigma_{\mathcal{D}}/2^\tau$