Revocable Privacy

Niels Feij, Henk Berendsen, Thomas de Haan



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Privacy versus Security

Privacy or security:

- Security and privacy are both important
- Strong security \rightarrow weak privacy and vice versa
- Security seems to be winning
- Giving up privacy for tempting reasons
- Examples?



Patriot Act

• Signed in 2001 - 45 days after 9/11

SURVEILLANCE UNDER THE PATRIOT ACT

Hastily passed 45 days after 9/11 in the name of national security...

The Patriot Act was the first of many changes to surveillance laws that made it easier for the government to spy on ordinary Americans by expanding the authority to monitor phone and email communications, collect bank and credit reporting records, and track the activity of innocent Americans on the Internet. While most Americans think it was created to catch terrorists, the Patriot Act actually turns regular citizens into suspects.



Patriot Act

- Signed in 2001 45 days after 9/11
- NSLs





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Patriot Act

- Signed in 2001 45 days after 9/11
- NSLs
- Sneak & peaks





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Between 2003 and 2005, the FBI made ${\bf 53}$ reported criminal referrals to prosecutors as a result of ${\bf 143,074}$ NSLs.

143,074 NSLs

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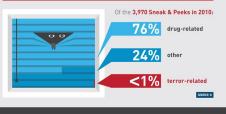
53 REPORTED CRIMINAL REFERRALS:



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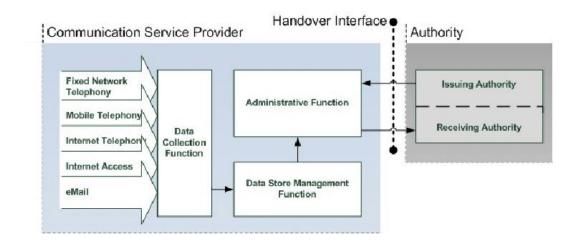
"Sneak & Peek" Searches:

The Patriat Act allows federal law enforcement agencies to delay giving notice when they conduct secret searches of Americans' homes and offices a fundamental change to Fourth Amendment privacy protections and search warrants. This means that government agents can enter a house, apartmen or office with a search warrant when the occupant is away, search through his/her property and take photographs—in some cases seizing property and electronic communications—and not tell the owner until later.



European data retention directive

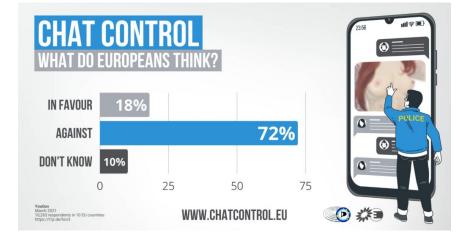
- Passed in 2006 by EU
- Telecommunication metadata
- Invalidated by European court of justice in 2014
- Many countries still kept the national laws





Child sexual abuse regulation (CSAR)

- Proposed in 2022
- Fight CSAM and Online grooming
- Proposal includes a form of client side scanning
- What are risks?
- Still no decision
- Lots of backlash
- Prof. Zuiderveen Borgesius





Security & Privacy

Combining security and privacy:

- A false contradiction
- Privacy while maintaining security
- Security for companies and services
- Safe and usable platforms without giving up all privacy
- Revocable privacy



What is revocable privacy?



What is revocable privacy: Formal definition

Definition

Property:

Data related to users who do not break any rule, is irrelevant. These users should stay anonymous as if no data was ever collected. [Lueks et al. 2016]

Definition:

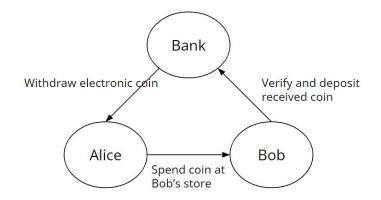
Users of a system are guaranteed to be anonymous unless they violate a predefined rule



Digital cash

Untraceable Electronic Cash [Chaum et al.]

- Online cash system
- First type of cryptographic electronic currency
- Alice is fully unlinkable to Bank

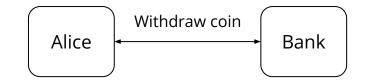






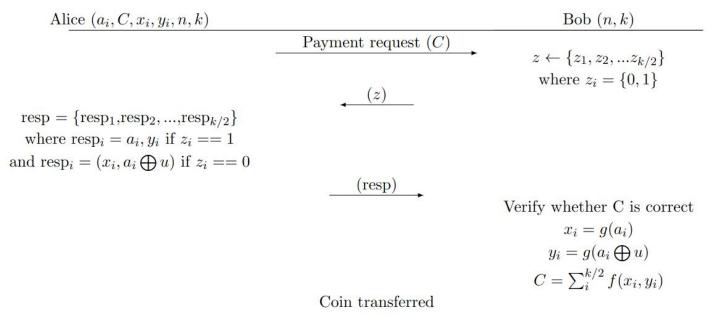
Alice withdraws a coin:

- Bank creates security parameter k ullet
- Alice creates k times some secret variables, amongst which is a۲
- Functions f, g behave like random oracle •
- Alice has a bank account number u.
- Alice extracts coin $C = \sum_{i}^{k/2} f(x_i, y_i)$ •
- $x_i = g(a_i)$ $y_i = g(a_i \oplus u)$





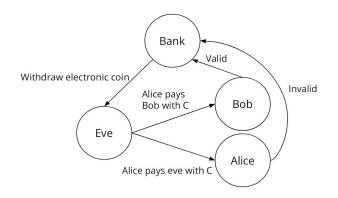
Alice pays Bob

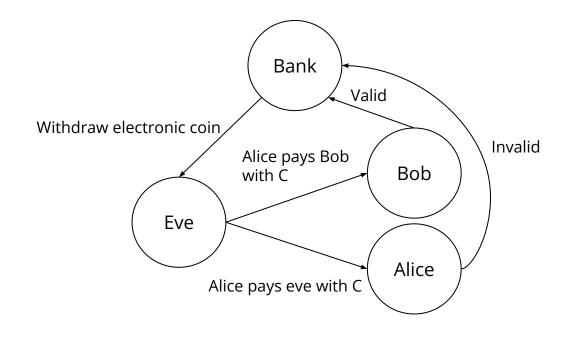


Digital cash

Multiple spending:

- Instead of Alice, Eve withdraws a coin and pays bob
- What if she spends C in another store?
- Other store will also create binary string $\,z'$
- If there exists an i such that $z_i' \neq z_i$
- The bank can find Eve's bank account : $a_i \oplus (a_i \oplus u) = u$







Anonymity

Different levels of anonymity:

- Fully identifiable
 - Users full identity can be easily uncovered
- Pseudonymity
 - Users full identity is hidden but still linkable
- Unlinkability
 - User is fully anonymous and no two actions are linkable



Anonymity

Object

What level of anonymity?

- Email address (without name):
- Licence Plate:
- Anonymous bank account:
- Cash:

Pseudonymity

Fully identifiable

Pseudonymity

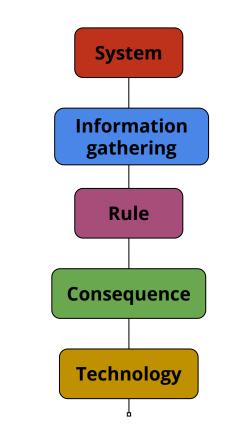
Unlinkability



What is revocable privacy: Set-up

What does it look like

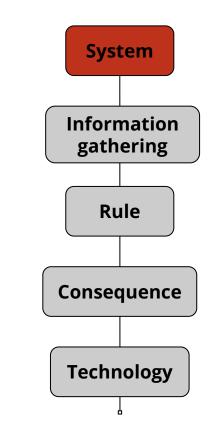
- 1. System with guaranteed anonymity
- 2. Method of information gathering
- 3. Rule (what constitutes misbehaviour?)
- 4. Consequence
- 5. Technology



What is revocable privacy: System

What does it look like

- 1. System with guaranteed anonymity:
 - Technical vs policy • Function creep
 - Provided anonymity
 - Pseudonymity
 - Unlinkability
 - Can be toward other users
 - Depends on method of information gathering



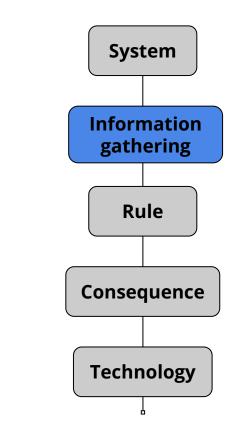


What is revocable privacy: Information gathering

What does it look like

2. Method of information gathering:

- Plaintext logging
 - Identity & relevant actions stored
 - Check rules against stored data
 - Policy related
 - Third parties
- Non-interactive sensors
 - Actions and Identities are visible
 - Encrypted based on rule
 - Nothing stored in plaintext
 - Trust in key management and proper behaviour
- Interactive sensors
 - User interaction
 - Fully anonymous
 - Trust in the users instead of sensor



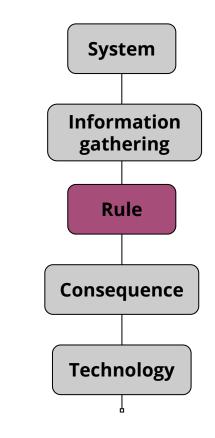
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What is revocable privacy: Rule

What does it look like

3. **Rule**

- Definition of misbehaviour
- What was the rule in electronic cash?
- Pre-defined
 - Ideally known to users
 - Configurable parameters
- Multiple different classes of rules
- To be continued...

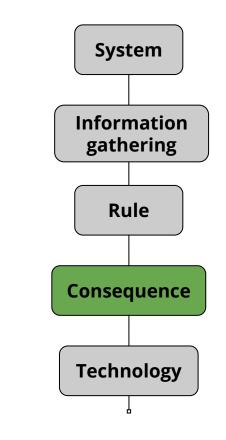


What is revocable privacy: Consequence

What does it look like

4. Consequence

- Revoking of privacy ۲
 - Revoking privacy to the company/service
 - Revoking privacy to other users •
- Blocking (can anyone think of an example?) ۰
 - Platform wide
 - Localized



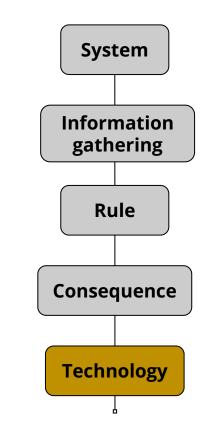


What is revocable privacy: Technology

What does it look like

5. Technology

- Actively researched
- Often cryptographic in nature
- To be continued...





The Rules



Use Cases / Rules: Overview

Overview of rules [Lueks et al. 2016]

Threshold Rules

If action performed \geq k times, then ...

Predicate Rules

Logical AND formula of variables *If A and B and C, then ...*

Decision rules

Rules with human influence *If A is offensive, then ...*

Complex rules

Complex data (graphs, labels) or auxiliary data



Threshold rules

What

Threshold for actions within given period of time

When

Simple cases, relatively easy to implement

How

Distributed encryption, n-times Anonymous Credentials, Transaction based Pseudonyms



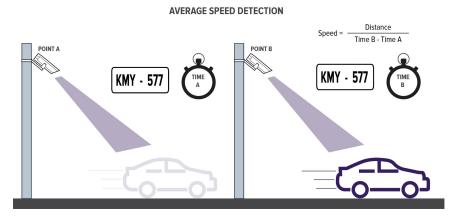
Use Cases / Rules: Threshold rules - Use case

Average speed checking

Case

Police wants to identify drivers that go over the speed limit on a given route

- Information gathering: Non-interactive sensor (camera)
- **Rule:** No more than 1 measurement within timeframe
- Consequence: Licence plate is revealed
- Technology: Distributed Encryption





Distributed encryption

The primitive allows a recipient of a message to decrypt it only if enough senders encrypted that same message.

- Tool to implement revocable privacy [Hoepman and Galindo]
- Senders have to be trusted
- Recovering plaintext is exponential





Key-evolving Distributed Encryption [Lueks et al., 2014]

- Proposed more efficient schemes
 - to handle short time frames
 - to handle high observation numbers

Uses

- Lagrange coefficients
- k-out-of-n Shamir secret sharing



Lagrange coefficients

For a set $\, I \subseteq \{1, \dots, n\}$ and field $\, \mathbb{Z}_q$ with $\, q > n$,

We define: Lagrange polynomials $\lambda_i^I(x)$ as $\lambda_i^I(x) = \prod_{t \in I \setminus \{i\}} \frac{x-t}{i-t} \in \mathbb{Z}^*_q[x]$ Lagrange coefficients as $\lambda_i^I = \lambda_i^I(0)$

Then: For any polynomial $P \in \mathbb{Z}_q[x]$ of degree at most |I|-1 ,

$$P(x) = \sum_{i \in I} P(i) \lambda^I_i(x) \qquad \quad P(0) = \sum_{i \in I} P(i) \lambda^I_i$$



Lagrange coefficients cont.

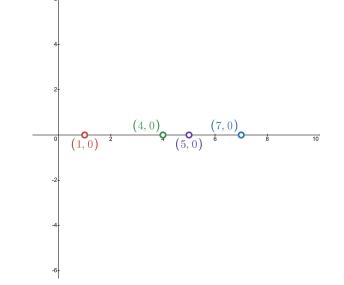
Let $I = \{1, 4, 5, 7\}$ and the field \mathbb{Z}_{10} such that q > n holds

For each $i \in I$ we compute the the *lagrange polynomial* $\lambda_i^I(x)$

$$\lambda_1^I(x) \ = \ \prod_{t \ \in I \setminus \{1\}} rac{x-t}{i-t} = rac{(x-4)(x-5)(x-7)}{(1-4)(1-5)(1-7)} \in \mathbb{Z}^*{}_q[x]$$

And lagrange coefficient λ_i^I

$$\lambda_1^I = \lambda_i^I(0) = rac{(0-4)(0-5)(0-7)}{(1-4)(1-5)(1-7)} = 1rac{17}{18}$$





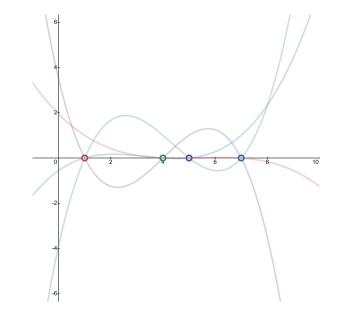
Lagrange coefficients cont.

For any polynomial $P \in \mathbb{Z}_q[x]$ of degree at most |I| - 1, $P(x) = \sum_{i \in I} P(i)\lambda_i^I(x)$ $P(0) = \sum_{i \in I} P(i)\lambda_i^I$ Let $P(x) = \frac{1}{2}x^3 - 2x^2 + 1$ such that $\deg(P) \le |I| - 1$ $3 \le 4 - 1$

Then:

$$P(x) = P(1)\lambda_1^I(1) + P(4)\lambda_4^I(4) + P(5)\lambda_5^I(5) + P(7)\lambda_7^I(7)$$

 $P(0) = P(1)\lambda_1^I + P(4)\lambda_4^I + P(5)\lambda_5^I + P(7)\lambda_7^I$





KDE: the idea

- Let G be a cyclic group of prime order q, such that DDH is hard in G
- Let $\chi: \{0,1\}^{l_p} \to G$, an injection encoding, and χ^{-1} , the inverse such that $\chi^{-1}(\chi(p)) = p$
 - This mapping is redundant
- Every sender *i* is given a secret share $s_i \in \mathbb{Z}_q$ which corresponds to a *k*-out-of-*n* Shamir secret sharing of a *publically known* value: 1
- Let f be the corresponding degree k-1 secret sharing polynomial, then f(0) = 1 and $s_i = f(i)$



KDE: the idea cont.

Ciphertext creation

- 1. Sender encodes plaintext into a generator: $\chi(p) \in G$
- 2. Sender uses secret share to produce ciphertext share: $\alpha_i = \chi(p)^{s_i}$

Given enough of these shares for the same plaintext, the exponents can be removed, and the original ciphertext can be recovered.

How?

- Consider a set $\{lpha_{i_1},\ldots,lpha_{i_k}\}$ of shares with $I=\{i_1,\ldots i_k\}$ the set of indices
- Then there exist Lagrange coefficients $\lambda_{i_1}^I, \dots, \lambda_{i_k}^I$ such that $\sum_{i \in I} \lambda_i^I s_i = f(0) = 1$
- So we can calculate $lpha = \prod_{i \in I} lpha_i^{\lambda_i^I} = \chi(p)^{\sum_{i \in I} s_i \lambda_i^I} = \chi(p)^{f(0)} = \chi(p)$



Use Cases / Rules: Threshold rules - Use case (2/2)

Server attack detection

Case

Server wants to detect and counter frequent fraudulent login attempts

- Information gathering: Plaintext logging (?)
- Rule: No more than *k* login attempts within timeframe *t*
- Consequence: IP address revealed
- Technology: Transaction based pseudonyms*





Transaction-based Pseudonyms [Biskup and Flegel]

Replaces personal identifiers by pseudonyms

If suspicious enough, identity can be recovered

Requires sensor to store records of events

Not truly revocable privacy, but best we've got



Predicate rules

What

- If A: Privacy secured If B: Privacy secured If A AND B: Privacy revoked
- Seemingly unrelated indicators

When

Often used in detecting criminal activity

How

Multiparty computation

Can you give an example?



Use Cases / Rules: Predicate rules - Use case

Car frauds

Case

Tax office wants to find fraudulent car users. Indicators:

- 1. Car is seen in traffic or public car park
- 2. Reported status of the car (work-only, not in use etc.)
- Information gathering: (non) Interactive sensor
- Rule: Both indicators must be true
- Consequence: License plate is revealed
- Technology: ???



Belastingdienst zet camera's in tegen belastingontduiker

De Belastingdienst wil automobilisten die motorrijtuigenbelasting (MRB) ontduiken vanaf volgend jaar opsporen via camerabeelden die op de openbare weg worden gemaakt. Dat blijkt uit het wetsvoorstel <u>'Overige</u> <u>Fiscale Maatregelen'</u> dat onderdeel is van de Prinsjesdagstukken.



Decision rules

What

- Rules that include Human Decision making
- Input to this decision can be from human or automatic sensors
- More sensitive and subjective topics

When

Useful in scenarios where the rule cannot be "codified"

How

Blacklistable Anonymous Credentials (BLAC), Group signatures



Use Cases / Rules: Decision rules - Use case (1/2)

Detecting child abuse

Case

Detecting child abuse by multiple authorities.

- Information gathering: Human input
- Rule: No more than *n* reports from different sources
- Consequence: Reveal child's identity
- Technology: Distributed encryption



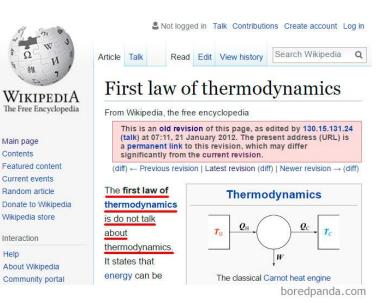


Use Cases / Rules: Decision rules - Use case (2/2) Anonymous editing

Case

Platform wants to prevent anonymous individuals from making wrong/fake edits

- Information gathering: Human input
- Rule: No more than *n* reports by moderators
- Consequence: User is anonymously blocked
- Technology: BLAC



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BlackListable Anonymous Credentials (BLAC) [Tsang et al.]

Idea

- User authenticates to Service Provider without revealing their identity
- Service Provider can deny access to misbehaving users by adding them to a blacklist

Involved parties

- User and Service Provider (SP)
- Group Manager (GM) issuing private *credentials* to users

Intuition

- User authenticates using private credential cred
- SP extracts *ticket* from authentication session's protocol transcript
- If user misbehaves, corresponding session's ticket is added to blacklist
- Authenticating user proves they did not generate a ticket on the blacklist



Complex rules

What

Rules that work with complex or extensive data

When

In cases of graphs, labels, large collateral information

How

- Can be described by any (difficult to define) deterministic computer program
- Lack of techniques



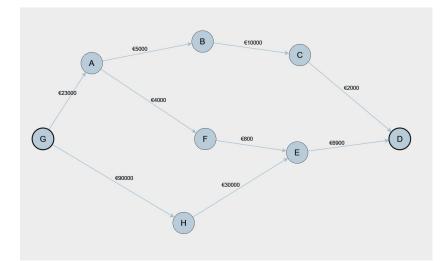
Use Cases / Rules: Complex rules - Use case

Cash flow anomaly

Case

Tax authority wants to detect cash fraud

- Information gathering: Interactive sensors
- Rule: In a graph of companies (nodes) and reported money flow (edges), money flow must be consistent.
- Consequence: Nodes identity is revealed
- Technology: Multiparty Computation





Use Cases / Rules: Complex rules - Technology Multiparty Computation

Multiple parties each have their own **private** input

Inputs used to compute a shared function of which only the output is shared

Computationally expensive

Successfully used to solve real world problems

Topic of final lecture



Use Cases / Rules - Conclusion

Privacy in practice

Is there active research on this? Are there real world implementations in use? Is it a known concept among big companies? Why?



Use Cases / Rules: Overview

Overview of rules [Lueks et al. 2016]

Threshold Rules

If action performed \geq k times, then ...

Predicate Rules

Logical AND formula of variables *If A and B and C, then ...*

Decision rules

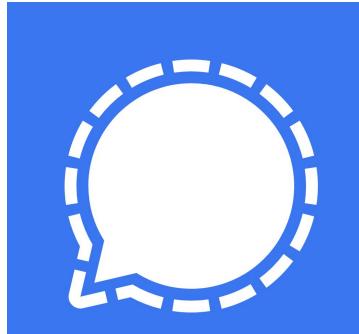
Rules with human influence *If A is offensive, then ...*

Complex rules

Complex data (graphs, labels) or auxiliary data









Signal: Overview

What is Signal?

- Messenger app
 - Like Whatsapp, Facebook Messenger etc.
- Open source



Signal: Overview

What is Signal?

- Messenger app
 - Like Whatsapp, Facebook Messenger etc.
- Open source
- Privacy friendly

Share Without Insecurity

State-of-the-art end-to-end encryption (powered by the open source Signal Protocol) keeps your conversations secure. We can't read your messages or listen to your calls, and no one else can either. Privacy isn't an optional mode — it's just the way that Signal works. Every message, every call, every time.



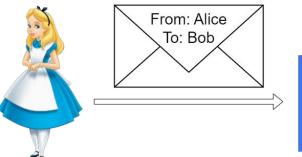
Signal's current privacy features

End-To-End Encryption

Signal cannot read your messages

Sealed Sender

Signal does not know who the message's sender is







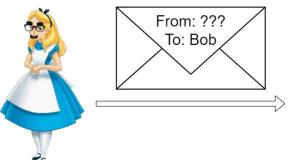
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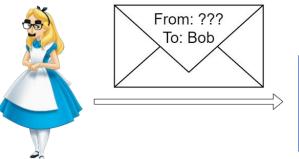
Signal cannot read your messages

Sealed Sender

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Private Group System

Signal does not know anything about your groups







Signal's Private Group System

Signal's solution

- Group state is stored encrypted on Signal server
- Symmetric encryption key *K* known only to group members

Blackboard example

• How does Alice create a group with Bob?



Signal's Private Group System

Signal's solution

- Group state is stored encrypted on Signal server
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Blackboard example

- How does Alice create a group with Bob?
- What if Eve tries to modify the group state?



Signal's Private Group System

Signal's solution

- Group state is stored encrypted on Signal server
- Symmetric encryption key *K* known only to group members

Blackboard example

- How does Alice create a group with Bob?
- What if Eve tries to modify the group state?
- **Problem:** Signal cannot authenticate users because group members are encrypted!
- Solution: Anonymous credentials
 - Group members prove their membership without revealing their identity



Signal Groups Privacy

- Great privacy with respect to Signal 😌
 - Signal doesn't know who you are talking with (Sealed Sender + Private Groups)
 - Signal doesn't know what you are talking about (E2E Encryption)
- Limited privacy with respect to other group members:
 - Phone number visible to group members
 - Other group members can easily identify you

Signal: Private phone number update

New update

- Username instead of phone number
- More anonymity towards other users:
 - Choose non-identifying username

Keep your phone number private with Signal usernames

Randall Sarafa on 20 Feb 2024

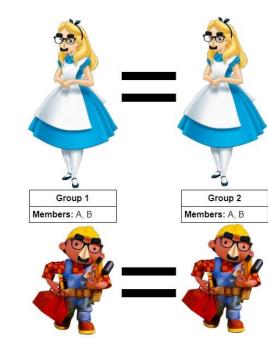


Signal's mission and sole focus is private communication. For years, Signal has kept your messages private, your profile information (like your name and profile photo) private, your contacts private, and your groups private – among much else. Now we're taking that one step further, by making your phone number on Signal more private.



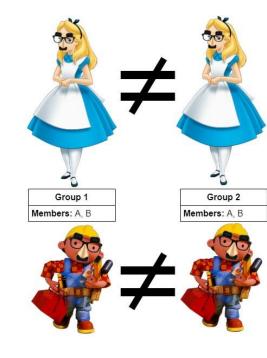
User anonymity in new update

- User achieves *pseudonymity* with respect to group members:
 - User cannot be identified by username
 - **But:** actions across groups are *linkable*
 - Link could be exploited to track the user across groups



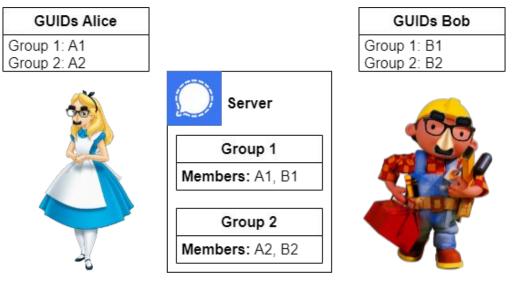
User anonymity in new update

- User achieves *pseudonymity* with respect to group members:
 - User cannot be identified by username
 - **But:** actions across groups are *linkable*
 - Link could be exploited to track the user across groups
 - Ideally, this link does not exist



Our proposal: Signal+

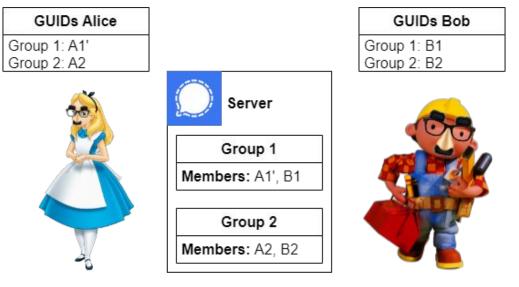
• Instead of a global UID, user has a separate GUID for each group





Our proposal: Signal+

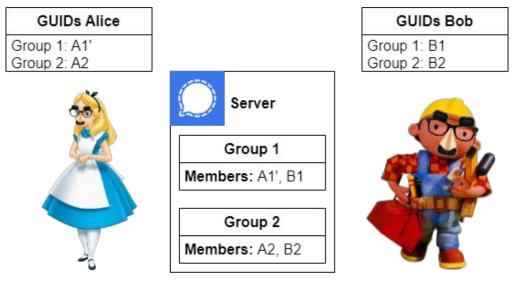
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Our proposal: Signal+

• Instead of a global UID, user has a separate GUID for each group



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• Any problems if Alice wants to remove Bob from a group?

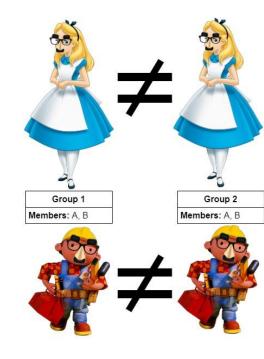
Our proposal: Signal+

Unlinkability across groups

- Instead of a fixed UID, user has a separate identity for each group
 - We call this identity the GUID
- Cross-group tracking no longer possible
- User can change identity in case of deanonymization

New challenges in Signal+

- Suppose Alice in a group with Eve
 - Alice and Eve are known by GUIDs A and E
- Eve is being malicious, so Alice wants to remove her from the group
- How can Alice remove Eve?





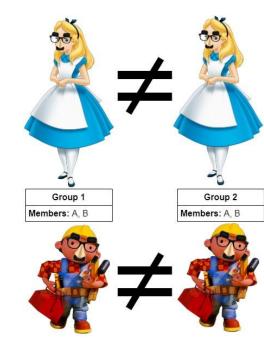
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- How can Alice remove Eve?
 - Suppose Alice removes E





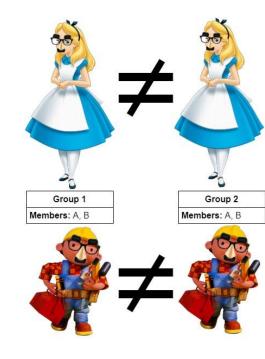
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Unlinkability across groups

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New challenges in Signal+

- Suppose Alice in a group with Eve
 - Alice and Eve are known by GUIDs A and E
- Eve is being malicious, so Alice wants to remove her from the group
- How can Alice remove Eve?
 - Suppose Alice removes E
 - Eve can just rejoin with a new identity!





Problem in Signal+ groups

Problem Description

- Group members only know each other's GUID
- Users can circumvent being removed from a group by changing their GUID

Solution

- We have a conflict of interests:
 - Benign users want to stay anonymous to Signal and group members
 - Signal and group members want to permanently block malicious users.
- Sounds like we need revocable privacy:
 - Rule: no more than 0 reports by group admin
 - Consequence: user is anonymously blocked from group



Recap of BLAC

- Involves user, Service Provider (SP) and Group Manager (GM)
- User registers with GM to obtain private credential cred
- SP keeps track of a blacklist of *tickets*
 - Each authentication session results in a ticket
 - Ticket can be added to blacklist if corresponding user misbehaved
- To authenticate, user proves they did not generate a ticket on the blacklist



Crypto behind BLAC: multiplicative groups

- Four multiplicative groups $\mathbb{G}, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_T$ of order p
- Generators $g_0, g_1, g_2 \in \mathbb{G}_1$ and $h_0 \in \mathbb{G}_2$
- Bilinear function $\hat{e} : \mathbb{G}_1 \times \mathbb{G}_2 \to \mathbb{G}_T$
 - Bilinearity: $\hat{e}(A^x, B^y) = \hat{e}(A, B)^{xy}$
- Group manager has a key-pair (*gsk*, *gpk*):
 - $gsk = \gamma$ chosen randomly from \mathbb{Z}_p
 - $\bullet \quad gpk \, = w = \, h_0^\gamma$
- User Alice has credential cred = (A, e, x, y)



Crypto behind BLAC: issuing credentials

Alice		GM $(gsk = \gamma, gpk = w = h_0^{\gamma})$
$x, y' \stackrel{\$}{\leftarrow} \mathbb{Z}_p$	<u> </u>	$m \xleftarrow{\$} \{0,1\}^\ell$
$C \leftarrow g_1^x g_2^{y'}$		
$r, s \xleftarrow{\$} \mathbb{Z}_p$		
$\operatorname{com} \leftarrow g_1^r g_2^s$		
$ch \leftarrow H(m, com)$		
$\mathrm{resp}_1 \leftarrow r + \mathrm{ch} \cdot x$		
$\mathrm{resp}_2 \gets s + \mathrm{ch} \cdot y'$	$\underbrace{(C, \operatorname{com}, \operatorname{resp}_1, \operatorname{resp}_2)}_{\bullet}$	$\operatorname{com} \cdot C^{\operatorname{ch}} \stackrel{?}{=} g_1^{\operatorname{resp}_1} \cdot g_2^{\operatorname{resp}_2}$
		$e, y'' \xleftarrow{\$} \mathbb{Z}_p$
$y \leftarrow y' + y''$	(A, e, y'')	$A \leftarrow (g_0 C g_2^{y''})^{\frac{1}{e+\gamma}}$
$(A \dots Le) ? (\dots x \cdot y \cdot L)$		

 $\hat{e}(A, wh_0^e) \stackrel{?}{=} \hat{e}(g_0 g_1^x g_2^y, h_0)$



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$r, s \xleftarrow{\$} \mathbb{Z}_p$		
$\operatorname{com} \leftarrow g_1^r g_2^s$		
$ch \leftarrow H(m, com)$		
$\mathrm{resp}_1 \leftarrow r + \mathrm{ch} \cdot x$	$\mathrm{com}\cdotC^{\mathrm{ch}}=g_1^rg_2^s\cdot\left(g_1^xg_2^{y'} ight)$	$\mathcal{G}^{\mathrm{ch}}=g_1^rg_2^s\cdot g_1^{\mathrm{ch}\cdot x}g_2^{\mathrm{ch}\cdot y'}=g_1^{\mathrm{r+ch}\cdot x}g_2^{s+\mathrm{ch}\cdot y'}=g_1^{\mathrm{resp}_1}\cdot g_2^{\mathrm{resp}_2}.$
$\operatorname{resp}_2 \leftarrow s + \operatorname{ch} \cdot y'$	$(C, \operatorname{com}, \operatorname{resp}_1, \operatorname{resp}_2)$	$\overset{ ext{ch}}{=} = g_1^r g_2^s \cdot g_1^{ ext{ch} \cdot x} g_2^{ ext{ch} \cdot y'} = g_1^{ ext{r+ch} \cdot x} g_2^{s+ ext{ch} \cdot y'} = g_1^{ ext{resp}_1} \cdot g_2^{ ext{resp}_2}$
		$e, y'' \xleftarrow{\$} \mathbb{Z}_p$
$y \leftarrow y' + y''$	(A, e, y'')	$A \leftarrow (g_0 C g_2^{y^{\prime\prime}})^{\frac{1}{e+\gamma}}$
$\hat{a}(A, a, be) \stackrel{?}{=} \hat{a}(a, a^{x}a^{y}b)$		

 $\hat{e}(A, wh_0^e) \stackrel{?}{=} \hat{e}(g_0 g_1^x g_2^y, h_0)$



Crypto behind BLAC: issuing credentials

Alice		GM $(gsk = \gamma, gpk = w = h_0^{\gamma})$
$x, y' \xleftarrow{\$} \mathbb{Z}_p$	<u> </u>	$m \xleftarrow{\$} \{0,1\}^\ell$
$C \leftarrow g_1^x g_2^{y'}$		
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$\operatorname{com} \leftarrow g_1^r g_2^s$		
$ch \leftarrow H(m, com)$		
$\operatorname{resp}_1 \leftarrow r + \operatorname{ch} \cdot x$		
$\mathrm{resp}_2 \gets s + \mathrm{ch} \cdot y'$	$(C, \operatorname{com}, \operatorname{resp}_1, \operatorname{resp}_2)$	$\bullet \operatorname{com} \cdot C^{\operatorname{ch}} \stackrel{?}{=} g_1^{\operatorname{resp}_1} \cdot g_2^{\operatorname{resp}_2}$
		$e, y'' \xleftarrow{\$} \mathbb{Z}_p$
$y \leftarrow y' + y''$	(A, e, y'')	$A \leftarrow (g_0 C g_2^{y''})^{\frac{1}{e+\gamma}}$
$\widehat{e}(A, wh_0^e) \stackrel{?}{=} \widehat{e}(g_0 g_1^x g_2^y, h_0)$)	
$\hat{e}(A,wh_{0}^{e})=\hat{e}igg(igg(g_{0}^{y^{\prime\prime}}Cg_{2}^{y^{\prime\prime}})$	$\left(ig)^{rac{1}{e+\gamma}}, h_0^\gamma h_0^e ight) = \hat{e} \left(\left(g_0 C g_2^{y''} ight)^{rac{1}{e+\gamma}} ight)^{rac{1}{e+\gamma}}$ Radboud University	$\hat{e}_{1}^{rac{1}{r\gamma}},h_{0}^{e+\gamma}igg)=\hat{e}\left(g_{0}g_{1}^{x}g_{2}^{y'}g_{2}^{y''},h_{0} ight)^{rac{e+\gamma}{e+\gamma}}=\hat{e}\left(g_{0}g_{1}^{x}g_{2}^{y},h_{0} ight)^{rac{1}{r\gamma}}$

Crypto behind BLAC: issuing credentials

Alice		GM $(gsk = \gamma, gpk = w = h_0^{\gamma})$
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$\hat{e}(A, wh_0^e) \stackrel{?}{=} \hat{e}(g_0 g_1^x g_2^y, h_0)$		

At the end of the protocol, Alice has obtained her credential cred = (A, e, x, y)Radboud University

Crypto behind BLAC: authentication

Scenario

- User Alice with cred = (A, e, x, y) authenticates towards SP Bob
- Bob has a blacklist $BL = \langle au_1, \dots, au_n
 angle$
 - Ticket au_i consists of a *serial* $s_i \in \{0,1\}^\ell$ and *tag* $t_i \in \mathbb{G}$
- Hash function $H_0: \{0,1\}^* o \mathbb{G}$

Authentication

- Bob sends (BL, m) with $m \stackrel{\$}{\leftarrow} \{0, 1\}^{\ell}$ a random message
- Alice computes the *bases* $b_i = H_0(s_i || ext{Bob})$ and a new ticket $\tau = (s, H_0(s || ext{Bob})^x)$
- Alice proves in zero knowledge:
 - 1. Her credential is valid: $\hat{e}(A, wh_0^e) = \hat{e}\left(g_0g_1^xg_2^y, h_0
 ight)$
 - 2. She is not blacklisted: $t_i \neq b_i^x$ for all i
 - 3. Her new ticket is valid: $t = H_0(s||\text{Bob})^x$

Applying BLAC to Signal+

Involved parties

- Signal acts as Group Manager to issue credentials to its users
- Signal acts as Service Provider to let users interact with a group

Blacklist

- Each group has a blacklist of removed users
- To link users with new GUID to the blacklist, the GUID is a BLAC ticket
 - Even with new GUID, user cannot prove they *did not* generate a blacklisted ticket
- If a user is removed from a group, their GUID is added to the blacklist

Group access management

- Only group members are allowed to retrieve/modify group state
- Problem: Signal does not know identity of group members
- Solution: each group also has a **whitelist** of GUIDs:
 - User should prove to Signal that they *did* generate a whitelisted ticket

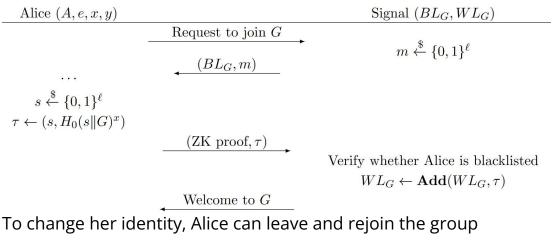


Signal+ group example

Scenario

Alice is a registered Signal user with credential cred = (A, e, x, y) who wants to join group G

Joining the group





Signal+ group messaging

- Alice is now part of *G*, but how does she receive a group message?
 - In the context of the group, both Signal and group members do not know her UID
- Solution: Signal stores look-up table of (GUID, UID) pairs
 - To maintain unlinkability, GUIDs are hashed with a keyed hash function
 - After joining G with GUID τ , Alice asks Signal to add $(H(K_G||\tau), Alice)$
- Bob sending a group message to (among others) Alice:
 - 1. Bob retrieves τ from WL_G
 - 2. Bob asks Signal to send a message to the UID corresponding to $H(K_G||\tau)$
 - 3. Signal uses the look-up table and forwards the message to Alice



Signal+ group example

Scenario

Bob wants to join Alice's group, and has the symmetric group key K

Joining the group

- 1. Bob anonymously authenticates towards Signal, and requests to join group
- 2. Ticket from this authentication session will be his GUID B
- 3. Bob has to prove he did not generate any tickets on the group's blacklist:
 - If Bob is blacklisted, authentication fails
 - Otherwise, Signal adds his GUID to the whitelist
- 4. Bob adds himself to the group members list

Sending group messages

- Signal maintains lookup table of hashed GUID UID pairs
- Bob asks Signal to add (H(K || B), Bob)
- Group members can message Bob by computing *H(K || B)*



Signal+: Conclusion

Signal+ group anonymity

- User's identity in a group (GUID) is a different BLAC ticket in each group
 - BLAC tickets are unlinkable and non-invertible
- Group members only know each other's GUIDs
 - Unlinkability with respect to other users is achieved
- Signal also has a lookup table of pairs $(H(K_G || \text{GUID}), \text{UID})$
 - If *H* is cryptographically secure, Signal cannot derive the GUID from the digest
 - Unlinkability with respect to Signal is achieved



Signal+: Conclusion

Signal+ reflection

- Can Signal+ unlinkability be improved?
- Are there scenarios where users *can* be linked?







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